

# Model-Based Dynamic Optimization with OpenModelica and CasADi

---

**Alachew Shitahun**

PELAB – Programming Environment Lab, Dept. Computer Science  
Linköping University, SE-581 83 Linköping, Sweden

**Vitalij Ruge**

Mathematics and Engineering, University of Applied Sciences Bielefeld

**Moritz Diehl**

Dept. of Electrical Engineering and Optimization in Engineering Center  
(OPTEC), K.U. Leuven, Belgium

**5th OpenModelica Workshop**

**February 4, 2013**

**Linköping**

# Outline of Presentation

---

1. Motivation
2. Optimization with Modelica
3. OpenModelica and CasADi
4. XML Code Generation in OpenModelica
5. Optimization Tool Chain for OpenModelica and CasADi
6. Test Cases and Results
7. Conclusions
8. Questions

# Motivation

---

- ▶ **Modelica** enable users to conveniently model large-scale physical systems
  - ▶ Traditionally used for simulation
- ▶ Nonlinear optimal control problems (NOCP) based on differential-algebraic equations (DAE)
  - ▶ State-of-the-art methods are using numerical algorithms
- ▶ Many other possible usages of the model
  - ▶ For example dynamic optimization for NOCP
- ▶ Current Modelica tools mainly focused on simulation, but recently also optimization
  - ▶ Dymola supports parameter and design optimization of models written in Modelica whereas
  - ▶ JModelica.org and OpenModelica have native support for optimal control.

# Optimization with Modelica

---

- ▶ Modelica has strong support for modeling of dynamic systems
- ▶ Additional elements for optimization:
  - ▶ Cost function
  - ▶ What to optimize (Variables and Parameters) and
  - ▶ Constraints
- ▶ Optimica language extension:
  - ▶ Extension of Modelica.
  - ▶ Enables formulation of optimization problems in Modelica models.
- ▶ How ?
  - ▶ Export Models in XML from OpenModelica and Import to CasADi

# OpenModelica and CasADi

---

## ▶ OpenModelica

- ▶ Modelica-based modeling and simulation platform
- ▶ Support optimica extension
- ▶ Extended with XML export of models based on standardized XML schema for models
- ▶ The XML export also includes the Optimica extension

## ▶ CasADi

- An open-source framework for numerical optimization developed by *KU Leuven*
- Enable users to implement optimal control algorithms with a wide range of methods, including
  - Multiple shooting and
  - Collocation
- Imports XML for dynamic optimization

# XML Code Generation in OpenModelica

- Modelica models are first flattened.
- XML schema structure mapped to the abstract syntax tree of OpenModelica compiler
- Text template based implementation of the code generation to XML

```
optimization VDP_Opt (objective = cost(finalTime),
                    startTime = 0 finalTime = 20)

parameter Real p1 = 1;
parameter Real p2 = 1;
parameter Real p3 = 2;

Real x1(start = 0);
Real x2(start = 1);

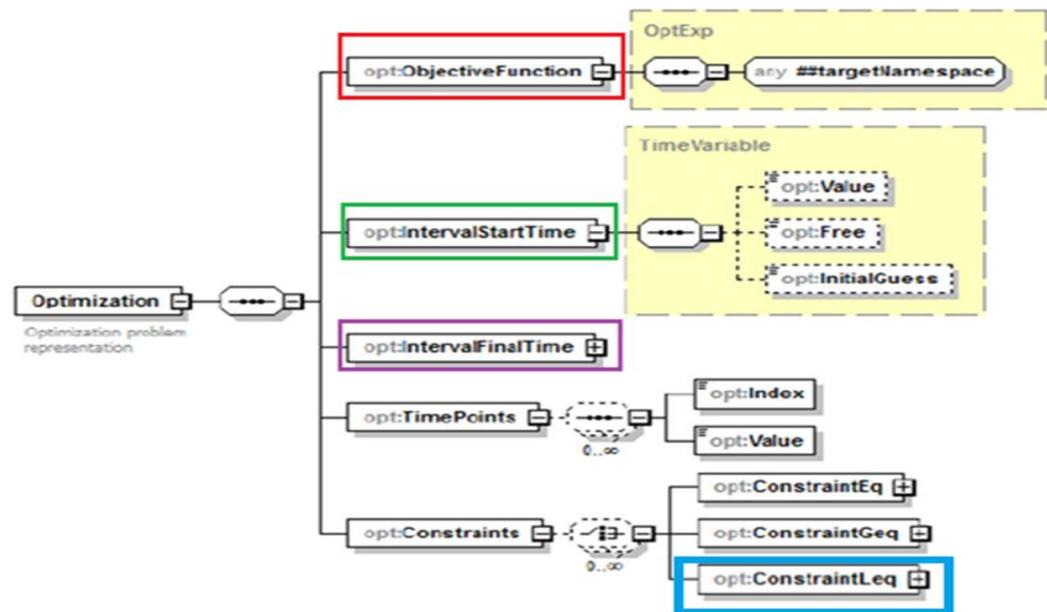
input Real u;

Real cost(start=0);

equation
der(x1) = (1 - x2 ^ 2) * x1 - x2 + u;
der(x2) = p1 * x1;
der(cost)=exp(p3*1/*time*/) * (x1^2 + x2^2 + u^2);

constraint u<=0.75;

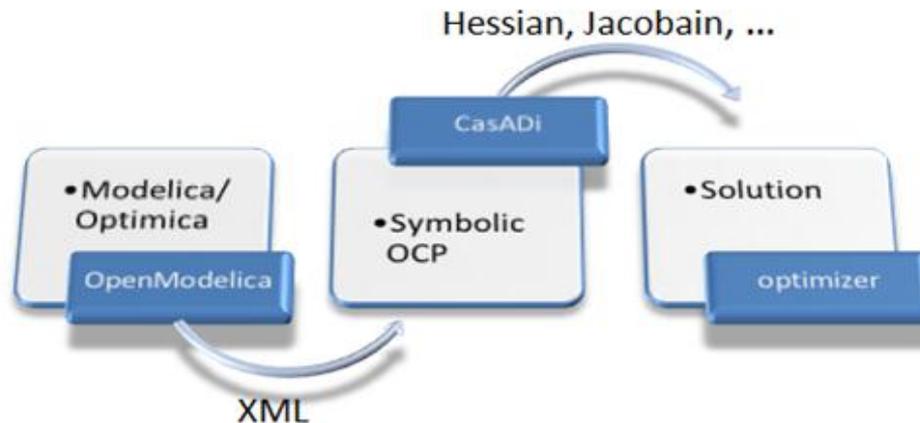
end VDP_Opt;
```



# Optimization Tool Chain for OpenModelica and CasADi

---

- **Export** of model from OpenModelica platform
- **Import** the model in CasADi
- **Solve** optimization problem in CasADi



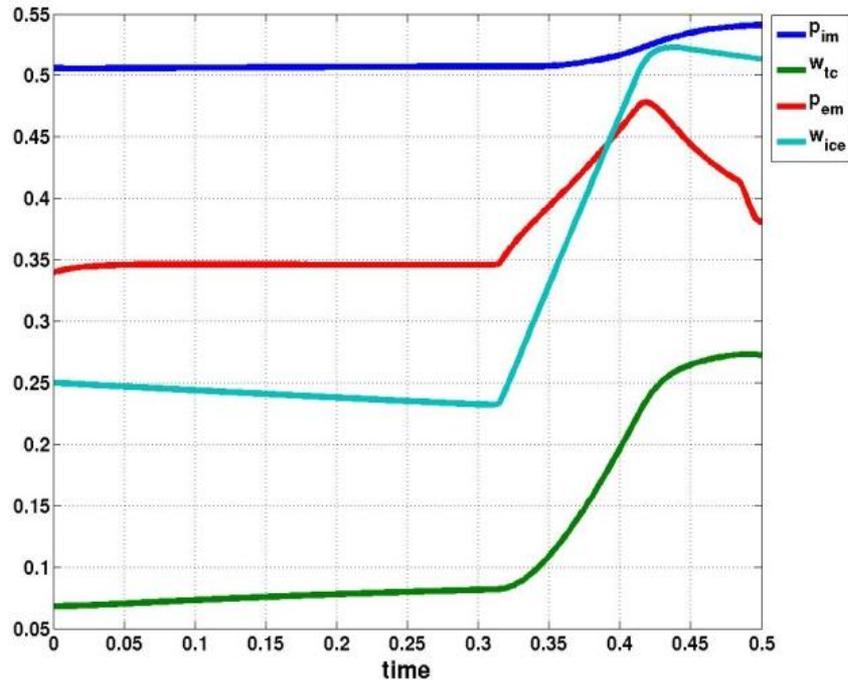
# Test Cases - Diesel Electric Powertrain

---

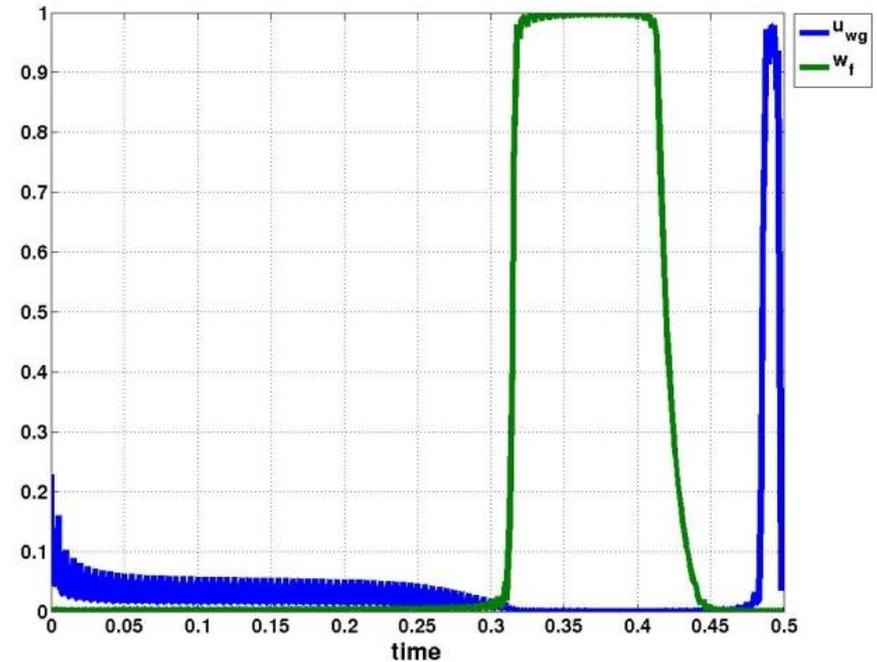
- Presented by
  - **Martin Sivertsson** and **Lars Eriksson**. (2012)
  - **Bernhard Bachmann** and et al. (2012).
- Nonlinear mean value engine model (MVEM)
- Find fuel optimal control and state trajectories from idling condition to a certain power level
- Mathematical problem formulation:
  - 2 inputs ( $u_f, u_{wg}$ )
  - 4 states ( $\omega_{ice}, p_{im}, p_{em}, \omega_{tc}$ )
  - 32 algebraic equations
- The problem solved here is a minimum fuel problem for a transient from idle to 170 kW, in a certain time interval  $[0, 0.5]$ .

# Results- Diesel Electric Powertrain

State variables ( $\omega_{ice}, p_{im}, p_{em}, \omega_{tc}$ )



Control variables ( $u_f, u_{wg}$ )



- Engine is accelerated only near the end of the time interval to meet the end constraints while minimizing the fuel consumption

# Conclusions

---

- Model-based dynamic optimization with OpenModelica and CasADi has been demonstrated on three industrial use cases.
- The OpenModelica platform coupling with CasADi demonstrates the use of an XML-based model exchange format for model-based optimization with OpenModelica

# References

---

- Alachew Shitahun, Vitalij Ruge, Mahder Gebremedhin, Bernhard Bachmann, Lars Eriksson, Joel Andersson, Moritz Diehl, Peter Fritzson. Model-Based Optimization with OpenModelica and CasADi. Subm: 7th IFAC Symp. on Advances in Automotive Control.
- Alachew Shitahun. Template Based XML and Modelica Unparsers in OpenModelica. Master thesis. Linkoping University, August 30, 2012
- Roberto Parrotto, Johan Åkesson, and Francesco Casella. An XML representation of DAE systems obtained from continuous-time Modelica models. In 3rd Int. Workshop on Equation-based Object-Oriented Modeling Languages and Tools - EOOLT 2010, Sept. 2010.
- Johan Åkesson. Languages and Tools for Optimization of Large-Scale Systems. Ph.D. Thesis, Lund University, Nov 2007.

# References

---

- Joel Andersson, Johan Åkesson and Moritz Diehl. CasADi --A symbolic package for automatic differentiation and optimal control, Recent Advances in Algorithmic Differentiation, Lecture Notes in Computational Science and Engineering Volume 87: 297-307, 2012.
- Martin Sivertsson and Lars Eriksson. (2012). Time and Fuel Optimal Power Response of a Diesel-Electric Powertrain. E-CoSM'12 – IFAC Workshop on Engine and Powertrain Control, Simulation and Modeling, 2012.
- Bernhard Bachmann and et al. (2012). Parallel Multiple-Shooting and Collocation Optimization with OpenModelica. In Pro. Of 9th International Modelica Conference. Munich, Germany pp. 659, Sept 3-5, 2012.

# Questions

---

Thank you !!

